

Circular economy innovations in a 2-area input-output stock-flow consistent dynamic model

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European Commission Grant, Project 101003491: “A Just Transition to the Circular Economy” (JUST2CE)

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 - o a **systematic review** of current literature on macroeconomic models for assessing the transition towards a CE
 - o a **formal model** (or set of models) to simulate and compare alternative CE policies and transition scenarios

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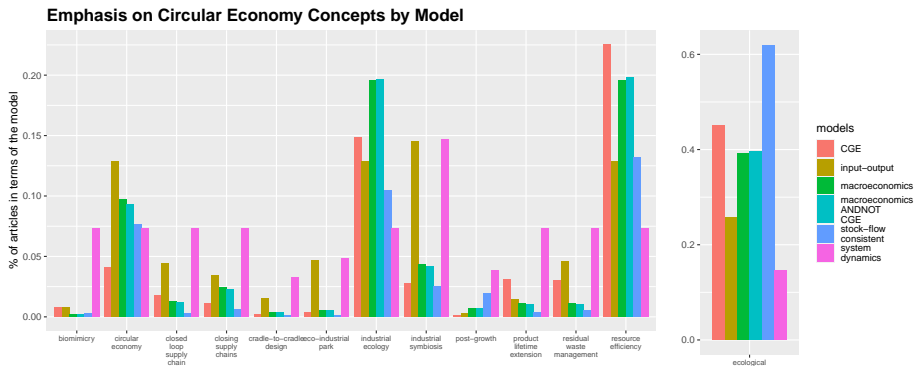
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- We have identified, discussed, and assessed the most popular/promising tools (to model the transition...)

FIGURE A1. CONCEPTS AND MODELS



Source: Valles-Codina et al. (2022)

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 - 2) **SFC models**. PROS: dynamics, finance. CONS: homogeneous output
- In principle, we can disaggregate SFC models by crossbreeding them with IO models... (**Hardt and O'Neill 2017**)

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 - 2) To assess the impact of a simple CE innovation on the economy, the society and the ecosystem

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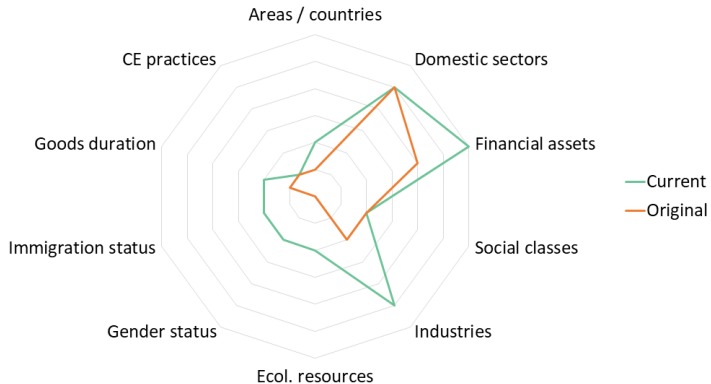
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- d) Solution: numerical simulations (*R* code), 100 periods, 100 iterations

FIGURE 1. MODEL DIMENSIONS



ASSETS AND LIABILITIES

TABLE 1: Balance-sheet matrix in period 20 (curr. p., EU currency)

	EU					<i>xr</i>	RoW					Tot	
	H	F	G	B	CB		H	F	G	B	CB		
Money	62.21				-62.21	1	83.47					-83.47	0.00
Advances						1							0.00
Deposits	372.61			-372.61		1	499.46			-499.46			0.00
Loans	-13.33	-85.00		98.33		1	-17.03	-111.45		128.48			0.00
EU bills	23.31		-926.45	274.27	613.21	1	15.65						0.00
RoW bills	11.66				-551.01	1	31.30		53.61	370.98	83.47		0.00
EU shares	9.32	-9.95				1	0.63						0.00
RoW shares	0.47					1	12.52	-12.99					0.00
Capital stock		94.95				1		124.44					219.39
Net financial wealth	-466.24		926.45			1	-625.99		-53.61				-219.39
Total	0.00	0.00	0.00	0.00	0.00		0.00	0.00	0.00	0.00	0.00	0.00	0.00

TRANSACTIONS AND Δ IN STOCKS

TABLE 2: Transactions-flow matrix in period 20 (curr. p., EU currency)

	EU						xr	RoW						Tot	
	H	F (y)	F (k)	G	B	CB		H	F (y)	F (k)	G	B	CB		
Consumption	-621.39	621.39					1	-837.43	837.43						0.00
Investment		6.65	-6.65				1		9.28	-9.28					0.00
Government spending		180.8		-180.80			1		181.09		-181.09				0.00
Export of EU		86.84					1		-86.84						0.00
Import of EU		-112.01					1		112.01						0.00
[Value added]		[769.61]					1		[1034.5]						0.00
Wage bill	455.42	-455.42					1	568.70	-568.7						0.00
Corporate profit	303.47	-306.22					1	458.15	-455.4						0.00
Amortization		-4.65	4.65				1		-6.06	6.06					0.00
Bank profit	7.44				-7.44		1	9.93				-9.93			0.00
CB profit				2.49		-2.49	1				3.32			-3.32	0.00
Income tax revenue	-153.55			153.55			1	-207.73			207.73				0.00
VAT revenue		-6.15		6.15			1		-8.29		8.29				0.00
Tariffs revenue		-7.89		10.18			1		-10.18		7.89				0.00
Interests on deposits	7.44				-7.44		1	9.93				-9.93			0.00
Interests on loans	-0.50	-3.32			3.82		1	-0.64	-4.33			4.97			0.00
Interests on EU bills	0.93			-35.31	11.06	22.69	1	0.62							0.00
Interests on RoW bills	0.47					-20.20	1	1.25			0.29	14.88	3.32		0.00
Change in money stock	0.04						1	-0.38						0.38	0.00
Change in advances							1								0.00
Change in deposits	-0.53				0.53		1	-3.13				3.13			0.00
Change in loans	0.73		2.00		-2.73		1			3.16		-4.16			0.00
Change in EU bills	0.01			43.73	2.20	-45.88	1	-0.07							0.00
Change in RoW bills	0.01					45.91	1	-0.14			-46.43	1.03	-0.38		0.00
Change in EU shares	0.01						1								0.00
Change in RoW shares							1	-0.06		0.06					0.00
Revaluation effects							1								0.00
Total	0.00	0.00	0.00	0.00	0.00	0.00		0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00

CROSS-INDUSTRY INTERDEPENDENCIES

TABLE 3: Baseline: IO matrix in period 20 (curr. p., EU currency, no calibration)

	EU demand for inputs					RoW demand for inputs					Final dem.	Output
	M	A	S	W	R	M	A	S	W	R		
EU production												
Manufacturing	67.01	66.89	67.13	26.13	0.00	5.58	5.57	5.59	2.18	0.00	312.33	558.43
Agriculture	67.01	66.89	67.13	26.13	0.00	5.58	5.57	5.59	2.18	0.00	311.35	557.45
Services	67.01	66.89	67.13	26.13	0.00	5.58	5.57	5.59	2.18	0.00	313.31	559.41
Waste manag.	67.00	66.89	67.12	0.00	0.00	5.58	5.57	5.59	0.00	0.00	0.00	217.76
Recycling	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
RoW production												
Manufacturing	5.58	5.57	5.59	2.18	0.00	67.01	66.89	67.13	26.13	0.00	312.33	558.43
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Recycling	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00
Value added												
~ Compensation of employees	128.65	128.41	128.89	46.55	0.00	128.65	128.41	128.89	46.55	0.00		
~ G.O. surplus and mixed incomes	139.41	139.18	139.64	86.27	0.00	139.41	139.18	139.64	86.27	0.00		
Taxes on production	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00	0.00		
Output	558.43	557.45	559.41	217.76	0.00	558.43	557.45	559.41	217.76	0.00		

AREA-SPECIFIC PHYSICAL FLOWS

TABLE 4: Physical flow matrix in period 20 (matter = Gt, energy = EJ)

	EU matter	RoW matter	Global matter	EU energy	RoW energy	Global energy
Inputs						
Extracted matter	317.86	2141.84	2459.7			
Recycled matter	7.72	55.3	63.03			
Renewable energy			0	1176.34	1461.97	2638.31
Non-renewable energy	17.37	23.33	40.7	7204.01	8980.65	16184.66
Oxygen	46.37	62.3	108.66			
Outputs						
Industrial CO ₂ emissions	-63.73	-85.63	-149.36			
Discarded stock	-28.34	-276.51	-304.84			
Dissipated energy				-8380.36	-10442.61	-16760.72
Δ in socio-economic stock	297.24	1920.64	2217.88			
Difference	0	0	0	0	0	0

GLOBAL PHYSICAL STOCKS AND RELATED CHANGES

TABLE 5: Physical stock-flow matrix in period 20 (matter = Gt, energy = EJ)

	Material reserves	Energy reserves	CO ₂ concentration	Socio-economic stock
Initial stock	9451266.99	-201040.39	2101.05	40831.85
Resources converted into reserves	193156.73	1536.04		
CO ₂ emissions			149.36	
Production of material goods				2522.72
Extraction/use of matter/energy	-2459.7	-16184.66		
Distruction of socio-ec. stock				-304.84
Final stock	9647311.66	-197232.48	2442.4	37174.38
Difference	0	0	0	0

SELECTED EQUATIONS: HOUSEHOLDS

- Total “real” consumption in each area is:

$$c^z = \alpha_1^z \cdot \frac{YD_w^z}{E(p_A^z)} + \alpha_2^z \cdot \frac{YD_c^z}{E(p_A^z)} + \alpha_3^z \cdot \frac{V_{-1}^z}{p_{A,-1}^z} \quad (1)$$

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- Households' total disposable income in each area is:

$$\begin{aligned} YD^z = & WB^z + DIV^z + FB^z + \\ & + r_{m,-1}^z \cdot M_{h,-1}^z + r_{b,-1}^z \cdot B_{s,z,-1}^z + x r_{-1}^f \cdot r_{b,-1}^f \cdot B_{s,z,-1}^f + \\ & + \Delta x r^f \cdot (B_{s,z,-1}^f + E_{s,z,-1}^f) - r_{h,-1}^z \cdot L_{h,-1}^z - T^z \end{aligned} \quad (2)$$

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- Households' net wealth is:

$$V^z = V_{-1}^z + YD^z - c^z \cdot p_A^z \quad (3)$$

SELECTED EQUATIONS: FIRMS (CURRENT)

- Let us consider a 10×10 global production. The **final demand** vector of EU is:

$$\mathbf{d}^z = \begin{pmatrix} \beta_1^z \\ \vdots \\ \beta_{10}^z \end{pmatrix} \cdot c^z + \begin{pmatrix} \iota_1^z \\ \vdots \\ \iota_{10}^z \end{pmatrix} \cdot \tilde{I}_d^z + \begin{pmatrix} \sigma_1^z \\ \vdots \\ \sigma_{10}^z \end{pmatrix} \cdot gov^z + \begin{pmatrix} \eta_{1,z}^f \\ \vdots \\ \eta_{10,z}^f \end{pmatrix} \cdot exp^z - \begin{pmatrix} \eta_1^z \\ \vdots \\ \eta_{10}^z \end{pmatrix} \cdot imp^z \quad (4)$$

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- The **gross output** vector is:

$$\mathbf{x}^z = \mathbf{A} \cdot \mathbf{x}^z + \mathbf{d}^z = (\mathbf{I} - \mathbf{A})^{-1} \cdot \mathbf{d}^z, \text{ with } : \mathbf{A} = \begin{pmatrix} a_{1,1} & \cdots & a_{1,10} \\ \dots & \ddots & \dots \\ a_{10,1} & \cdots & a_{10,10} \end{pmatrix} \quad (5)$$

SELECTED EQUATIONS: FIRMS (CURRENT)

- Let us consider a 10×10 global production. The **final demand** vector of EU is:

$$\mathbf{d}^z = \begin{pmatrix} \beta_1^z \\ \vdots \\ \beta_{10}^z \end{pmatrix} \cdot c^z + \begin{pmatrix} \iota_1^z \\ \vdots \\ \iota_{10}^z \end{pmatrix} \cdot i_d^z + \begin{pmatrix} \sigma_1^z \\ \vdots \\ \sigma_{10}^z \end{pmatrix} \cdot gov^z + \begin{pmatrix} \eta_{1,z}^f \\ \vdots \\ \eta_{10,z}^f \end{pmatrix} \cdot exp^z - \begin{pmatrix} \eta_1^z \\ \vdots \\ \eta_{10}^z \end{pmatrix} \cdot imp^z \quad (4)$$

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- The **value added** in each area is:

$$YN^z = c^z \cdot p_A^z + i_d^z \cdot p_I^z + gov^z \cdot p_G^z + EXP^z - IMP^z - VAT^z - TAR^z \quad (6)$$

SELECTED EQUATIONS: CONSUMER CHOICES

- The share of manufacturing products to total consumption is stable:

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$$\beta_3^z = \beta_{3,-1}^z + \beta_{31}^z \cdot \frac{YD_{w,-1}^z}{p_{3,-1}^z} + \beta_{32}^z \cdot \frac{YD_{c,-1}^z}{p_{3,-1}^z} \quad (8)$$

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- The **share of agricultural products** is calculated residually, and tends to decline as the economy grows:

$$\beta_2^z = 1 - \beta_1^z - \beta_3^z \quad (9)$$

with $\beta_2^z \geq 0$.

SELECTED EQUATIONS: FIRMS (CAPITAL)

- The **target stock of fixed capital** depends on industry-specific target capital to output ratios:

$$k^{z*} = \mathbf{p}_{-1}^{zT} \cdot [\mathbf{h}^z \odot (\mathbf{x}_{-1}^z + \mathbf{x}_{-1}^f)] \cdot \frac{1}{p_{l,-1}^z} \quad (10)$$

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$$i_d^z = \gamma^z \cdot (k^{z*} - k_{-1}^z) + \delta^z \cdot k_{-1}^z \quad (11)$$

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$$i_d^z = \gamma^z \cdot (k^{z*} - k_{-1}^z) + \delta^z \cdot k_{-1}^z \quad (11)$$

- The end-of-period stock of **bank loans** is defined residually:

$$L_F^z = L_{F,-1}^z + i_d^z \cdot p_I^z - AF^z - FF_u^z - \Delta E_s^z \quad (12)$$

where:

$$AF^z = \delta^z \cdot k_{-1}^z \cdot p_I^z - k^z \cdot \Delta p_I^z$$

SELECTED EQUATIONS: COMMERCIAL BANKS

- The supply of bank loans is:

$$L_s^z = L_F^z + L_h^z \quad (13)$$

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- where the demand for personal loans is defined as:

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- The supply of bank deposits is:

$$M_s^z = M_h^z \quad (15)$$

SELECTED EQUATIONS: LABOUR MARKET AND POPUL.

- The **employment** generated by demand of (domestic and foreign) industries is:

$$N^z = \mathbf{x}^z T \cdot \mathbf{I}^z = \sum N_j^z \quad (16)$$

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- The available **labour force** in each area is:

$$\mathbf{POP}^z = \mathbf{POP}_{-1}^z \odot (I + \mathbf{g}_{pop}^z) + \mathbf{IMM}^z - \mathbf{IMM}^f \quad (17)$$

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- **Immigration** inflow in each area is:

$$\mathbf{IMM}^z = \gamma_{imm,0}^z \odot \mathbf{POP}_{-1}^f + \gamma_{imm,1}^z \odot \mathbf{un}_{-1}^f + \gamma_{imm,2}^z \odot (\mathbf{w}_{-1}^z - \mathbf{w}_{-1}^f) \quad (18)$$

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- In each industry, the **percentage of female workers** (gender segregation) is:

$$\rho_j^z = \rho_{0j}^z - \rho_{1j}^z \cdot (w_j^z - w_{j,-1}^z) \quad (19)$$

SELECTED EQUATIONS: GOVERNMENT AND CB

- The **government budget deficit** in each area is:

$$DEF_g^z = gov^z \cdot p_G^z + r_{b,-1}^z \cdot B_{s,-1}^z - F_{cb}^z - T^z - VAT^z - TAR^z \quad (20)$$

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- Therefore, the **supply of government bills** is:

$$B_s^z = B_{s,-1}^z + DEF_g^z \quad (21)$$

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- **Cash supply** adjusts to households' demand:

$$H_s^z = H_h^z \quad (23)$$

SELECTED EQUATIONS: PRICES

- Firms use a mark-up rule. The **unit price of production** vector is:

$$\mathbf{p}^{z*} = \mathbf{w}^z \odot \mathbf{l}^z + \mathbf{p}^{z*} \cdot \mathbf{A} \odot \mathbf{m}^{z*} \odot \mathbf{h}_d^z \quad (24)$$

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- However, **market prices** also depend on labour-constrained potential output, vat and tariffs:

$$\mathbf{p}^z = [\mathbf{p}^{z*} + \Gamma_x^z \odot (\mathbf{x}_{-1}^z - \mathbf{x}_{-1}^{z*})] \odot \left[\begin{pmatrix} 1 \\ \vdots \\ 1 \end{pmatrix} + \tau_{vat}^z + \tau_{tar}^f \right] \quad (25)$$

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- The consumer price index or **average price of consumption** is:

$$p_A^z = \mathbf{p}^{zT} \cdot \beta^z \quad (26)$$

SELECTED EQUATIONS: PORTFOLIO CHOICES

- Households' demand for domestic bills is:

$$\begin{aligned} \frac{B_{h,z}^z}{V^z} = & \lambda_{10} + \lambda_{11} \cdot r_{b,-1}^z - \lambda_{12} \cdot \left(r_{b,-1}^f + \frac{\Delta x r^f}{x r^f} \right) - \lambda_{13} \cdot r_{m,-1}^z - \lambda_{14} \cdot \frac{YD^z}{V^z} + \\ & - \lambda_{15} \cdot r_{e,-1}^z - \lambda_{16} \cdot \left(r_{e,-1}^f + \frac{\Delta x r^f}{x r^f} \right) \end{aligned} \quad (27)$$

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- Households' demand for cash is:

$$H_h^z = \lambda_c^z \cdot c_{-1}^z \cdot p_{A,-1}^z \quad (28)$$

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$$M_h^z = V^z + L_h^z - H_h^z - B_{h,z}^z - B_{h,z}^f - E_{h,z}^z - E_{h,z}^f \quad (29)$$

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- The redundant equation is:

$$B_{cb,z}^z = B_s^z - B_{s,z}^z - B_{s,f}^z - B_b^z$$

FIGURE 2. SANKEY DIAGRAM OF TRANSACTIONS (IN $t = 20$)

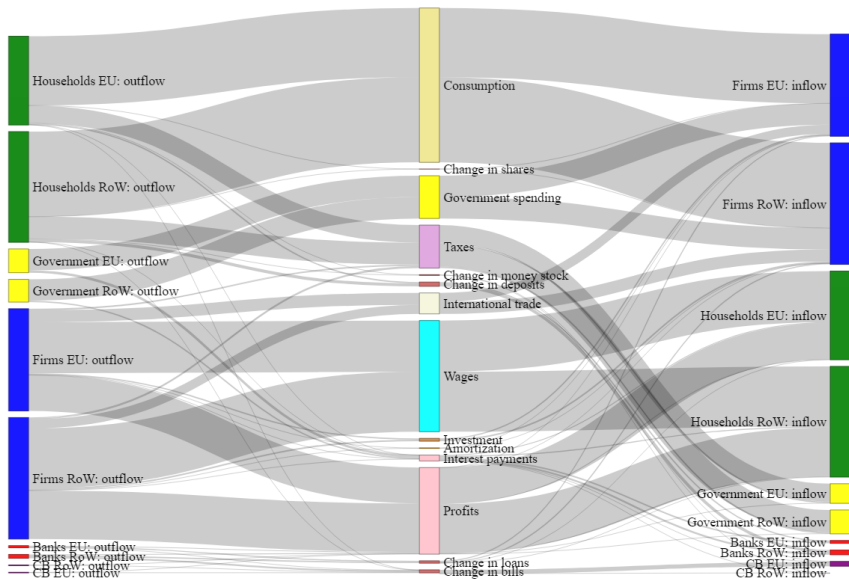


FIGURE 3. CROSS-INDUSTRY INPUT-OUTPUT FLOWS (IN $t = 20$)

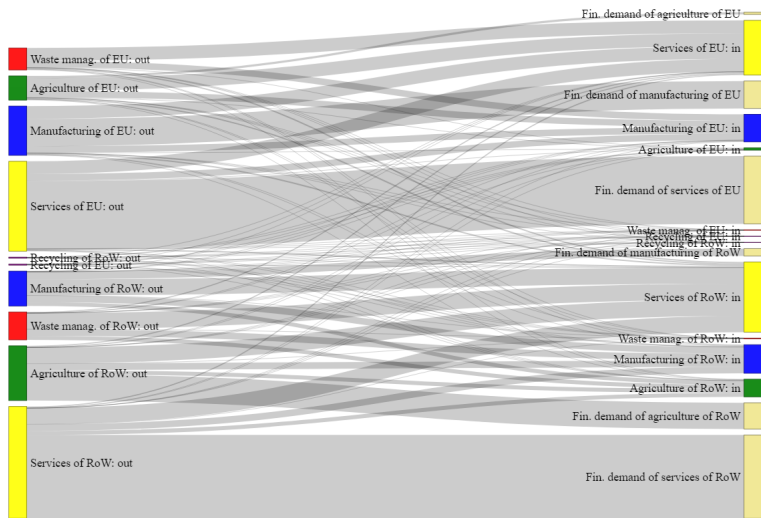


FIGURE 4. PHYSICAL FLOWS OF MATTER AND ENERGY (IN $t = 20$)

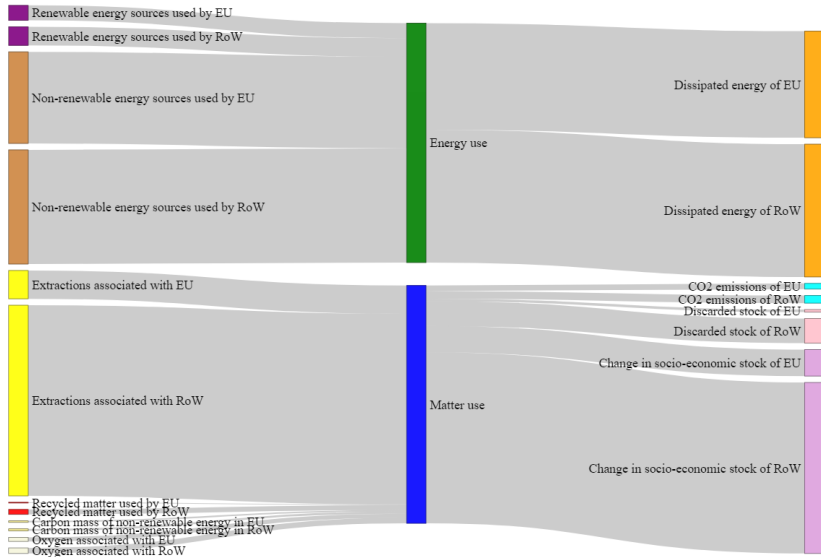


FIGURE 5. ADJUSTMENT OF SELECTED VARIABLES TO STEADY STATE

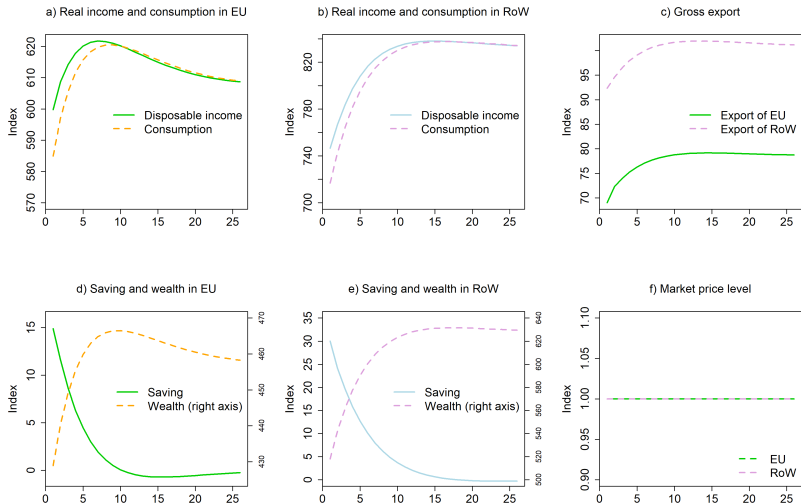
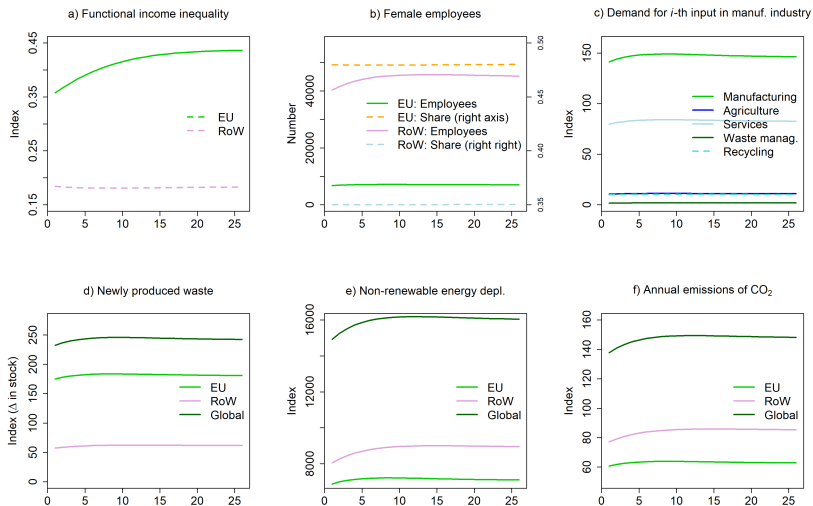


FIGURE 6. ADJUSTMENT OF SELECTED VARIABLES TO STEADY STATE



THE CIRCULAR ECONOMY (CE)

- CE = policies that aim at reusing, repairing, sharing, and recycling products and resources to create a **closed-loop system**, thus minimising waste, pollution, and CO₂ emissions

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- If waste is not recycled, the global matrix of technical coefficients is:

$$\mathbf{A} = \left(\begin{array}{cccc|cccc} a_{11} & a_{12} & a_{13} & a_{14} & 0 & a_{16} & a_{17} & a_{18} & a_{19} & 0 \\ a_{21} & a_{22} & a_{23} & a_{24} & 0 & a_{26} & a_{27} & a_{28} & a_{29} & 0 \\ a_{31} & a_{32} & a_{33} & a_{34} & 0 & a_{36} & a_{37} & a_{38} & a_{39} & 0 \\ a_{41} & a_{42} & a_{43} & a_{44} & 0 & a_{46} & a_{47} & a_{48} & a_{49} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ \hline a_{61} & a_{62} & a_{63} & a_{64} & 0 & a_{66} & a_{67} & a_{68} & a_{69} & 0 \\ a_{71} & a_{72} & a_{73} & a_{74} & 0 & a_{76} & a_{77} & a_{78} & a_{79} & 0 \\ a_{81} & a_{82} & a_{83} & a_{84} & 0 & a_{86} & a_{87} & a_{88} & a_{89} & 0 \\ a_{91} & a_{92} & a_{93} & a_{94} & 0 & a_{96} & a_{97} & a_{98} & a_{99} & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \end{array} \right)$$

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- A CE innovation implies a change in technical coefficients...

A SIMPLE CE INNOVATION IN EU

- The new matrix will be:

$$\mathbf{A}' = \left(\begin{array}{ccccc|cccc}
 a'_{11} \leq a_{11} & a'_{12} \leq a_{12} & a'_{13} \leq a_{13} & a'_{14} \leq a'_{14} & a'_{15} > 0 & a_{16} & a_{17} & a_{18} & a_{19} & 0 \\
 a'_{21} \leq a_{21} & a'_{22} \leq a_{22} & a'_{23} \leq a_{23} & a'_{24} \leq a'_{24} & a'_{25} > 0 & a_{26} & a_{27} & a_{28} & a_{29} & 0 \\
 a'_{31} \leq a_{31} & a'_{32} \leq a_{32} & a'_{33} \leq a_{33} & a'_{34} \leq a'_{34} & a'_{35} > 0 & a_{36} & a_{37} & a_{38} & a_{39} & 0 \\
 a'_{41} \leq a_{41} & a'_{42} \leq a_{42} & a'_{43} \leq a_{43} & a'_{44} \leq a'_{44} & a'_{45} > 0 & a_{46} & a_{47} & a_{48} & a_{49} & 0 \\
 a'_{51} > 0 & a'_{52} > 0 & a'_{53} > 0 & a'_{54} > 0 & 0 & a_{56} & a_{57} & a_{58} & a_{59} & 0 \\
 \hline
 a'_{61} \leq a_{61} & a'_{62} \leq a_{62} & a'_{63} \leq a_{63} & a'_{64} \leq a'_{64} & a'_{65} > 0 & a_{66} & a_{67} & a_{68} & a_{69} & 0 \\
 a'_{71} \leq a_{71} & a'_{72} \leq a_{72} & a'_{73} \leq a_{73} & a'_{74} \leq a'_{74} & a'_{75} > 0 & a_{76} & a_{77} & a_{78} & a_{79} & 0 \\
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 \end{array} \right)$$

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 a'_{21} \leq a_{21} & a'_{22} \leq a_{22} & a'_{23} \leq a_{23} & a'_{24} \leq a_{24} & a'_{25} > 0 & a_{26} & a_{27} & a_{28} & a_{29} & 0 \\
 a'_{31} \leq a_{31} & a'_{32} \leq a_{32} & a'_{33} \leq a_{33} & a'_{34} \leq a_{34} & a'_{35} > 0 & a_{36} & a_{37} & a_{38} & a_{39} & 0 \\
 a'_{41} \leq a_{41} & a'_{42} \leq a_{42} & a'_{43} \leq a_{43} & a'_{44} \leq a_{44} & a'_{45} > 0 & a_{46} & a_{47} & a_{48} & a_{49} & 0 \\
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 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
 \end{array} \right)$$

- Fall in coefficients defining the quantities of manufacturing and agricultural products and services used as inputs in first area (●)

A SIMPLE CE INNOVATION IN EU

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$$\mathbf{A}' = \left(\begin{array}{ccccc|cccc}
 a'_{11} \leq a_{11} & a'_{12} \leq a_{12} & a'_{13} \leq a_{13} & a'_{14} \leq a'_{14} & a'_{15} > 0 & a_{16} & a_{17} & a_{18} & a_{19} & 0 \\
 a'_{21} \leq a_{21} & a'_{22} \leq a_{22} & a'_{23} \leq a_{23} & a'_{24} \leq a'_{24} & a'_{25} > 0 & a_{26} & a_{27} & a_{28} & a_{29} & 0 \\
 a'_{31} \leq a_{31} & a'_{32} \leq a_{32} & a'_{33} \leq a_{33} & a'_{34} \leq a'_{34} & a'_{35} > 0 & a_{36} & a_{37} & a_{38} & a_{39} & 0 \\
 a'_{41} \leq a_{41} & a'_{42} \leq a_{42} & a'_{43} \leq a_{43} & a'_{44} \leq a'_{44} & a'_{45} > 0 & a_{46} & a_{47} & a_{48} & a_{49} & 0 \\
 a'_{51} > 0 & a'_{52} > 0 & a'_{53} > 0 & a'_{54} > 0 & 0 & a_{56} & a_{57} & a_{58} & a_{59} & 0 \\
 \hline
 a'_{61} \leq a_{61} & a'_{62} \leq a_{62} & a'_{63} \leq a_{63} & a'_{64} \leq a'_{64} & a'_{65} > 0 & a_{66} & a_{67} & a_{68} & a_{69} & 0 \\
 a'_{71} \leq a_{71} & a'_{72} \leq a_{72} & a'_{73} \leq a_{73} & a'_{74} \leq a'_{74} & a'_{75} > 0 & a_{76} & a_{77} & a_{78} & a_{79} & 0 \\
 a'_{81} \leq a_{81} & a'_{82} \leq a_{82} & a'_{83} \leq a_{83} & a'_{84} \leq a'_{84} & a'_{85} > 0 & a_{86} & a_{87} & a_{88} & a_{89} & 0 \\
 a'_{91} \leq a_{91} & a'_{92} \leq a_{92} & a'_{93} \leq a_{93} & a'_{94} \leq a'_{94} & a'_{95} > 0 & a_{96} & a_{97} & a_{98} & a_{99} & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
 \end{array} \right)$$

- Fall in coefficients defining the quantities of manufacturing and agricultural products and services used as inputs in first area (●)
- Domestic waste now enters the production process in first area (●)

A SIMPLE CE INNOVATION IN EU

- The new matrix will be:

$$\mathbf{A}' = \left(\begin{array}{ccccc|cccc}
 a'_{11} \leq a_{11} & a'_{12} \leq a_{12} & a'_{13} \leq a_{13} & a'_{14} \leq a_{14} & a'_{15} > 0 & a_{16} & a_{17} & a_{18} & a_{19} & 0 \\
 a'_{21} \leq a_{21} & a'_{22} \leq a_{22} & a'_{23} \leq a_{23} & a'_{24} \leq a_{24} & a'_{25} > 0 & a_{26} & a_{27} & a_{28} & a_{29} & 0 \\
 a'_{31} \leq a_{31} & a'_{32} \leq a_{32} & a'_{33} \leq a_{33} & a'_{34} \leq a_{34} & a'_{35} > 0 & a_{36} & a_{37} & a_{38} & a_{39} & 0 \\
 a'_{41} \leq a_{41} & a'_{42} \leq a_{42} & a'_{43} \leq a_{43} & a'_{44} \leq a_{44} & a'_{45} > 0 & a_{46} & a_{47} & a_{48} & a_{49} & 0 \\
 a'_{51} > 0 & a'_{52} > 0 & a'_{53} > 0 & a'_{54} > 0 & 0 & a_{56} & a_{57} & a_{58} & a_{59} & 0 \\
 \hline
 a'_{61} \leq a_{61} & a'_{62} \leq a_{62} & a'_{63} \leq a_{63} & a'_{64} \leq a_{64} & a'_{65} > 0 & a_{66} & a_{67} & a_{68} & a_{69} & 0 \\
 a'_{71} \leq a_{71} & a'_{72} \leq a_{72} & a'_{73} \leq a_{73} & a'_{74} \leq a_{74} & a'_{75} > 0 & a_{76} & a_{77} & a_{78} & a_{79} & 0 \\
 a'_{81} \leq a_{81} & a'_{82} \leq a_{82} & a'_{83} \leq a_{83} & a'_{84} \leq a_{84} & a'_{85} > 0 & a_{86} & a_{87} & a_{88} & a_{89} & 0 \\
 a'_{91} \leq a_{91} & a'_{92} \leq a_{92} & a'_{93} \leq a_{93} & a'_{94} \leq a_{94} & a'_{95} > 0 & a_{96} & a_{97} & a_{98} & a_{99} & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
 \end{array} \right)$$

- Fall in coefficients defining the quantities of manufacturing and agricultural products and services used as inputs in first area (●)
- Domestic waste now enters the production process in first area (●)
- Manufacturing and agricultural products and services are used as inputs in waste industry of first area (●)

THE ROLE OF THE GOVERNMENT SECTOR

- There is a tendency for current technical coefficients to converge to target CE values over time:

$$a_{ij} = a_{ij,-1} + \gamma_A^z \cdot (a'_{ij,-1} - a_{ij,-1}) \quad (30)$$

THE ROLE OF THE GOVERNMENT SECTOR

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$$\gamma_A^z = \gamma_{A0}^z + \Gamma_A^{zT} \cdot \sigma^z \cdot gov_{-1}^z \quad (31)$$

THE ROLE OF THE GOVERNMENT SECTOR

- There is a tendency for current technical coefficients to converge to **target CE values** over time:

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where γ_A is defined as:

$$\gamma_A^z = \gamma_{A0}^z + \Gamma_A^{zT} \cdot \sigma^z \cdot gov_{-1}^z \quad (31)$$

- The average **speed of convergence** of technical coefficients to their target values is a linear, positive function of industry-specific **government expenditures**

FIGURE 6. CE-ORIENTED GOV. SPENDING IN EU

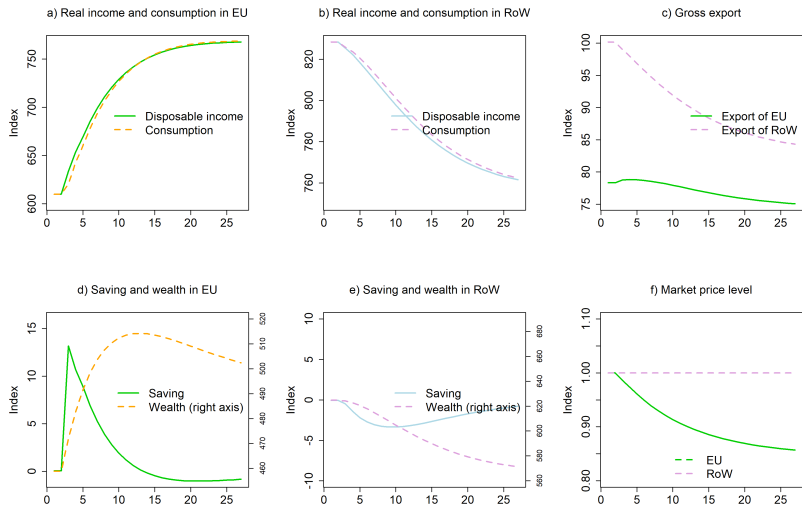
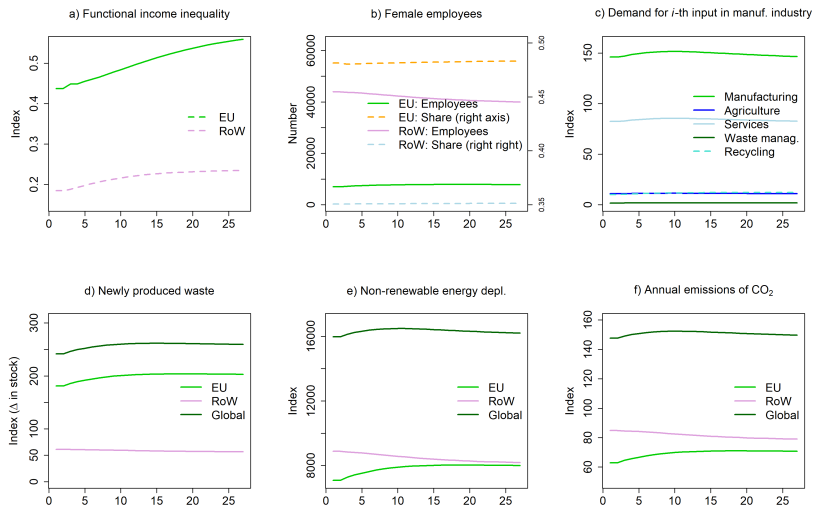


FIGURE 7. CE-ORIENTED GOV. SPENDING IN EU (CONT'D)



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FINAL REMARKS

- The model provides a **benchmark** for other MA-IO-SFC models
- Next steps:
 - a) Introduce landfill limit and consumption constraints
 - b) Make additional experiments
 - c) Complete calibration with real data (*Exiobase*) / estimate coefficients
 - d) Turn into n -area model

Thank you

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