

Circular economy in a simplified input-output stock-flow consistent model

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JUST2CE

A Just Transition to Circular Economy



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 - 2) To test a simple **CE innovation**

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- Solution: numerical simulations



NOMINAL VALUE OF ASSETS AND LIABILITIES

TABLE 1: Balance sheet in $t = 20$ (baseline)

	Households	Firms	Government	Central Bank	Total
Money	25.65	0	0.0	-25.65	0
Bills	2.85	0	-28.5	25.65	0
Net financial wealth	-28.50	0	28.5	0.00	0
Total	0.00	0	0.0	0.00	0

MONEY TRANSACTIONS AND CHANGES IN STOCKS

TABLE 2: Transactions-flow matrix in $t = 20$ (baseline)

	Households	Firms	Government	Central Bank	Total
Consumption	-25.86	25.86	0.00	0.00	0
Government spending	0.00	9.55	-9.55	0.00	0
Output	0.00	[35.41]	0.00	0.00	0
Wages and salaries	35.41	-35.41	0.00	0.00	0
Taxes	-7.08	0	7.08	0.00	0
Interest payments	0.05	0	-0.05	0.00	0
Change in money stock	-2.27	0	0.00	2.27	0
Change in bills	-0.25	0	2.52	-2.27	0
Total	0.00	0	0.00	0.00	0

MODEL EQUATIONS: (1)-(3)

- Total “real” consumption (constant prices) is:

$$c = \alpha_1 \cdot \frac{YD_{-1}}{p_{A,-1}} + \alpha_2 \cdot \frac{V_{-1}}{p_{A,-1}}$$

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where: $\mathbf{A} = \begin{pmatrix} a_{11} & a_{12} \\ a_{21} & a_{22} \end{pmatrix}$

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- If firms use a mark-up rule, the **price** vector is:

$$\mathbf{p} = w \cdot \mathbf{l} + \left[\begin{pmatrix} 1 \\ 1 \end{pmatrix} + \mathbf{m} \right] \odot \mathbf{A} \cdot \mathbf{p} \quad (6)$$



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- Households' disposable income is:

$$YD = Y_n + r \cdot B_{h,-1} - T \quad (10)$$

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- The **net wealth** of households is:

$$V = V_{-1} + YD - c \cdot p_A \quad (14)$$

MODEL EQUATIONS: (15)-(16)

- The private demand for bills is:

$$\frac{B_h}{V} = \lambda_0 + \lambda_1 \cdot r - \lambda_2 \cdot \frac{YD}{V}$$

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- Model IO-SIM is complete.

FIGURE 1. SANKEY DIAGRAM OF TFM

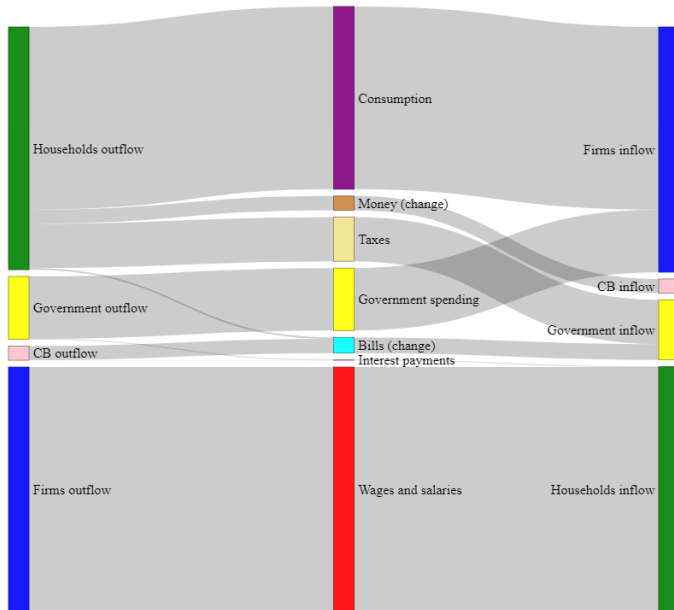
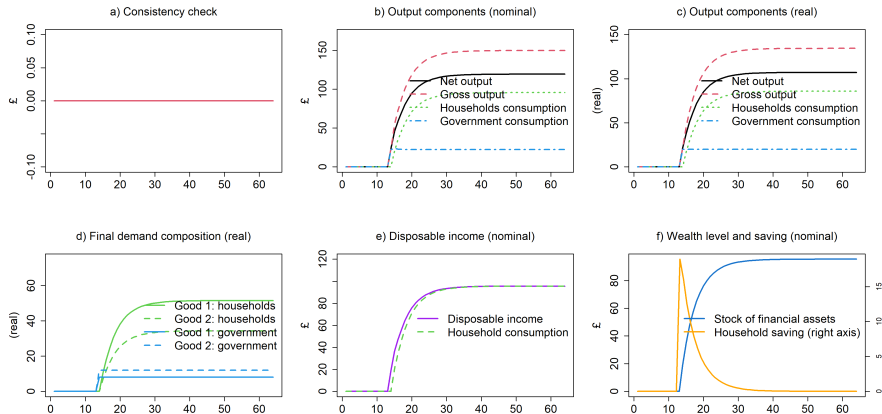


FIGURE 2. MODEL DYNAMICS: BASELINE



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where n is the number of rounds and t_0 is the period where the demand changes

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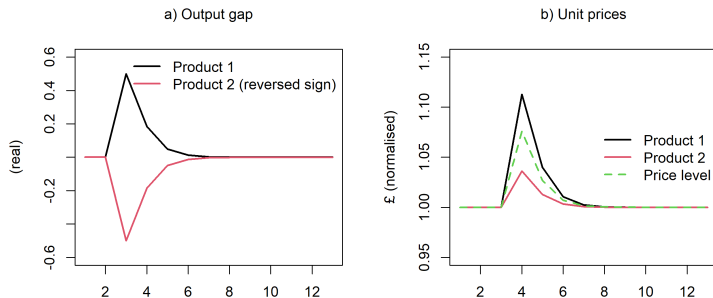
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- This captures temporary **demand pressures** on supply conditions

FIGURE 3. OUTPUT AND PRICE CHANGES AFTER A DEMAND SHOCK



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- CE implies a change in technical coefficients

FIGURE 4. PRODUCTION STRUCTURE WITHOUT CE

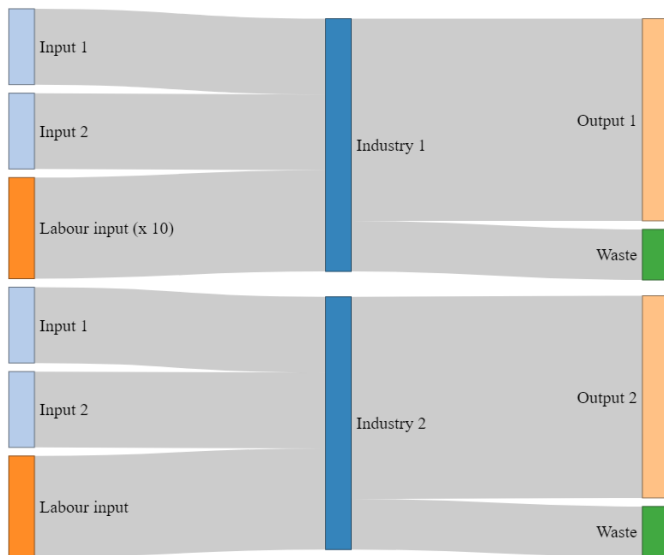
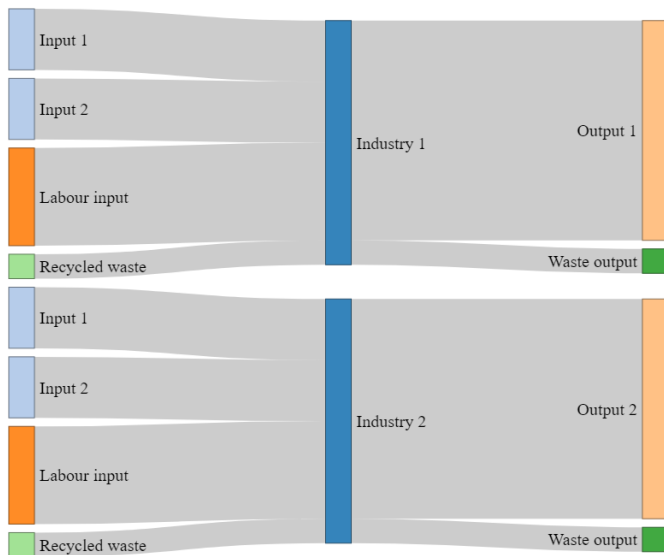


FIGURE 5. PRODUCTION STRUCTURE WITH (PARTIAL) CE



THE CIRCULAR ECONOMY (CONT'D)

- The new matrix will be:

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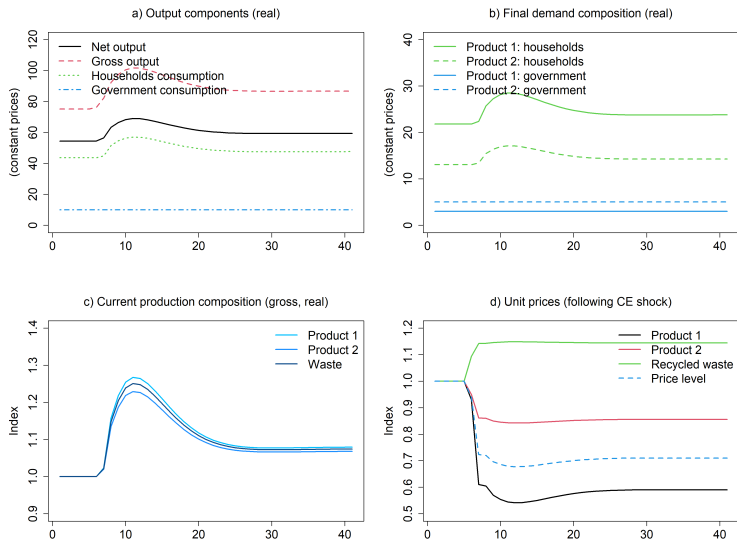
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- Mind the rebound effect!

FIGURE 6. CE POLICY IN A “2-INDUSTRY + WASTE” MODEL



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- A variety of feedback effects can be considered
- The main issue seems to be the consistency and availability of data...

Thank you

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