Circular economy in a simplified input-output stock-flow consistent model

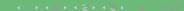
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"Link Campus" University of Rome & University of Leeds

14th Conference of the European Society for Ecological Economics

June 15th, 2022





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 - 2) To test a simple CE innovation



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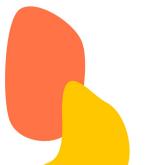
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- Solution: numerical simulations



Nominal value of assets and liabilities

Table 1: Balance sheet in t = 20 (baseline)

	Households	Firms	Government	Central Bank	Total
Money	25.63	0	0.00	-25.63	0
Bills	2.85	0	-28.48	25.63	0
Net financial wealth	-28.48	0	28.48	0	0
Total	0	0	0	0	0





Money transactions and changes in stocks

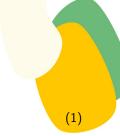
Table 2: Transactions-flow matrix in t = 20 (baseline)

	Households	Firms	Government	Central	Bank	Total
Consumption	-25.84	25.84	0		0	0
Government spending	0	9.55	-9.55		0	0
Output	0	[35.39]	0		0	0
Wages and salaries	35.39	-35.39	0		0	0
Taxes	-7.09	0	7.09		0	0
Interest payments	0.05	0	-0.05		0	0
Change in money stock	-2.26	0	0		2.26	0
Change in bills	-0.25	0	2.51		-2.26	0
Total	0	0	0		0	0



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$$c = \alpha_1 \cdot \frac{YD_{-1}}{p_{A,-1}} + \alpha_2 \cdot \frac{V_{-1}}{p_{A,-1}}$$







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- If firms use a mark-up rule, the price vector is:

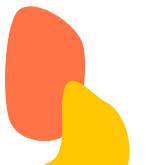
$$\mathbf{p} = w \cdot \mathbf{I} + \begin{bmatrix} 1 \\ 1 \end{bmatrix} + \mathbf{m} \odot \mathbf{A} \cdot \mathbf{p}$$
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- The deflator for household consumption is:

$$p_A = \mathbf{p}^T \cdot \mathbf{b} \tag{7}$$



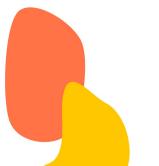


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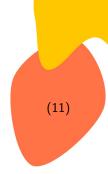
- Households' disposable income is:

$$YD = Y_n + r \cdot B_{h,-1} - T \tag{10}$$



- The supply of government bills is:

$$B_s = B_{s,-1} + g \cdot p_G - T$$



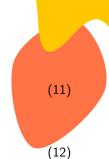


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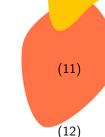
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- The net wealth of households is:

$$V = V_{-1} + YD - c \cdot p_A$$

(14)

(11)

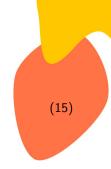
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- The private demand for bills is:

$$\frac{B_h}{V} = \lambda_0 + \lambda_1 \cdot r - \lambda_2 \cdot \frac{YD}{V}$$

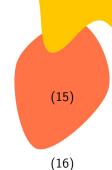


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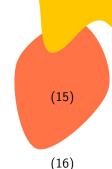
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- Model IO-SIM is complete.

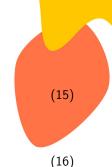




Figure 1. Sankey diagram of TFM (in t=20)

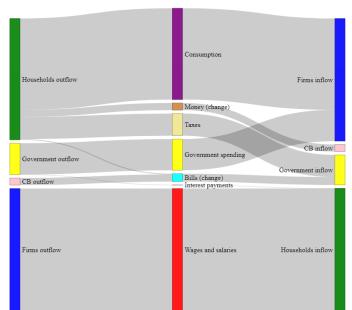
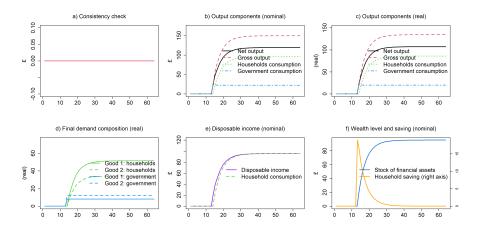


FIGURE 2. MODEL DYNAMICS: BASELINE



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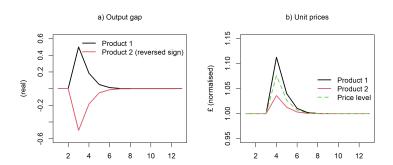
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- Therefore, mark-ups increase above their normal rates as long as current outputs fall short of (fully-adjusted) demand-implied outputs
- This captures temporary demand pressures on supply conditions





FIGURE 3. OUTPUT AND PRICE CHANGES AFTER A DEMAND SHOCK



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- CE implies a change in technical coefficients



FIGURE 4. PRODUCTION STRUCTURE WITHOUT CE

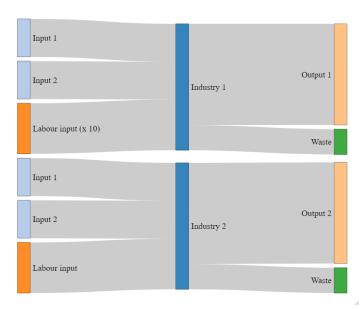
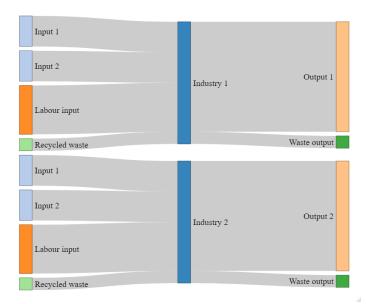


FIGURE 5. PRODUCTION STRUCTURE WITH (PARTIAL) CE



$$\mathbf{B} = \begin{pmatrix} b_{11} \le a_{11} & b_{12} \le a_{12} & b_{13} \ge 0 \\ b_{21} \le a_{21} & b_{22} \le a_{22} & b_{23} \ge 0 \\ b_{31} \ge a_{31} & b_{32} \ge a_{32} & 0 \end{pmatrix}$$





- The new matrix will be:

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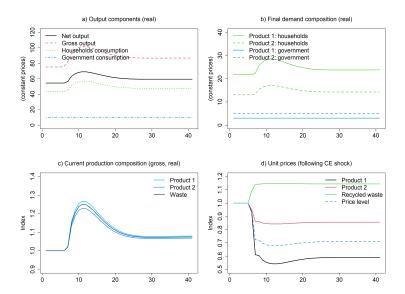


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- Mind the rebound effect!



FIGURE 6. CE POLICY IN A "2-INDUSTRY + WASTE" MODEL



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- A variety of feedback effects can be considered
- The main issue seems to be the consistency and availability of data...



Thank you

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